Mahesh Public School

Rational Numbers

Class 8

Worksheet - 4



1. Using appropriate properties find.

(i)
$$-\frac{2}{3} \times \frac{3}{5} + \frac{5}{2} - \frac{3}{5} \times \frac{1}{6}$$

(i)
$$-\frac{2}{3} \times \frac{3}{5} + \frac{5}{2} - \frac{3}{5} \times \frac{1}{6}$$
 (ii) $\frac{2}{5} \times \left(-\frac{3}{7}\right) - \frac{1}{6} \times \frac{3}{2} + \frac{1}{14} \times \frac{2}{5}$

2. Write the additive inverse of each of the following.

(i)
$$\frac{2}{8}$$

(ii)
$$\frac{-5}{9}$$

(i)
$$\frac{2}{8}$$
 (ii) $\frac{-5}{9}$ (iii) $\frac{-6}{-5}$ (iv) $\frac{2}{-9}$ (v) $\frac{19}{-6}$

(iv)
$$\frac{2}{-9}$$

(v)
$$\frac{19}{-6}$$

3. Verify that -(-x) = x for.

(i)
$$x = \frac{11}{15}$$

(i)
$$x = \frac{11}{15}$$
 (ii) $x = -\frac{13}{17}$

4. Find the multiplicative inverse of the following. (i) -13 (ii) $\frac{-13}{19}$ (iii) $\frac{1}{5}$ (iv) $\frac{-5}{8} \times \frac{-3}{7}$

(ii)
$$\frac{-13}{19}$$

(iv)
$$\frac{-5}{8} \times \frac{-3}{7}$$

(v)
$$-1 \times \frac{-2}{5}$$
 (vi) -1

5. Name the property under multiplication used in each of the following. (i) $\frac{-4}{5} \times 1 = 1 \times \frac{-4}{5} = -\frac{4}{5}$ (ii) $-\frac{13}{17} \times \frac{-2}{7} = \frac{-2}{7} \times \frac{-13}{17}$

(i)
$$\frac{-4}{5} \times 1 = 1 \times \frac{-4}{5} = -\frac{4}{5}$$

(ii)
$$-\frac{13}{17} \times \frac{-2}{7} = \frac{-2}{7} \times \frac{-13}{17}$$

(iii)
$$\frac{-19}{29} \times \frac{29}{-19} = 1$$

6. Multiply $\frac{6}{13}$ by the reciprocal of $\frac{-7}{16}$.

7. Tell what property allows you to compute $\frac{1}{3} \times \left(6 \times \frac{4}{3}\right)$ as $\left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$.

8. Is $\frac{8}{9}$ the multiplicative inverse of $-1\frac{1}{8}$? Why or why not?

9. Is 0.3 the multiplicative inverse of $3\frac{1}{3}$? Why or why not?

Write.

- The rational number that does not have a reciprocal.
- (ii) The rational numbers that are equal to their reciprocals.
- The rational number that is equal to its negative.
- 11. Fill in the blanks.

(i) Zero has _____ reciprocal.

(ii) The numbers _____ and ____ are their own reciprocals

(iii) The reciprocal of – 5 is ______.

(iv) Reciprocal of $\frac{1}{x}$, where $x \neq 0$ is _

(v) The product of two rational numbers is always a _____

(vi) The reciprocal of a positive rational number is _____

Answers of Worksheet - 4

Question 1:

Using appropriate properties find:

$$\frac{2}{3} \times \frac{3}{5} + \frac{5}{2} - \frac{3}{5} \times \frac{1}{6}$$

$$\frac{2}{5} \times \left(-\frac{3}{7}\right) - \frac{1}{6} \times \frac{3}{2} + \frac{1}{14} \times \frac{2}{5}$$

Answer:

(i)

$$-\frac{2}{3} \! \times \! \frac{3}{5} \! + \! \frac{5}{2} \! - \! \frac{3}{5} \! \times \! \frac{1}{6} \! = \! -\frac{2}{3} \! \times \! \frac{3}{5} \! - \! \frac{3}{5} \! \times \! \frac{1}{6} \! + \! \frac{5}{2}$$

(Using commutativity of rational numbers)

$$= \left(-\frac{3}{5}\right) \times \left(\frac{2}{3} + \frac{1}{6}\right) + \frac{5}{2}$$
 (Distributivity)

$$= \left(-\frac{3}{5}\right) \times \left(\frac{2 \times 2 + 1}{6}\right) + \frac{5}{2} = \left(-\frac{3}{5}\right) \times \left(\frac{5}{6}\right) + \frac{5}{2}$$

$$= \left(-\frac{3}{6}\right) + \frac{5}{2} = \left(\frac{-3 + 5 \times 3}{6}\right) = \left(\frac{-3 + 15}{6}\right)$$

$$= \frac{12}{6} = 2$$

$$\frac{2}{5} \times \left(-\frac{3}{7}\right) - \frac{1}{6} \times \frac{3}{2} + \frac{1}{14} \times \frac{2}{5} = \frac{2}{5} \times \left(-\frac{3}{7}\right) + \frac{1}{14} \times \frac{2}{5} - \frac{1}{6} \times \frac{3}{2}$$
 (By commutativity)

$$= \frac{2}{5} \times \left(-\frac{3}{7} + \frac{1}{14} \right) - \frac{1}{4}$$
 (By distributivity)

$$= \frac{2}{5} \times \left(-\frac{3 \times 2 + 1}{14} \right) - \frac{1}{4}$$

$$= \frac{2}{5} \times \left(-\frac{5}{14} \right) - \frac{1}{4}$$

$$= -\frac{1}{7} - \frac{1}{4}$$

$$= \frac{-4 - 7}{28} = \frac{-11}{28}$$

Question 2:

Write the additive inverse of each of the following:

(i)
$$\frac{2}{8}$$
 (ii) $\frac{-5}{9}$ (iii) $\frac{-6}{-5}$ (iv) $\frac{2}{-9}$ (v) $\frac{19}{-6}$

Answer:

(i)
$$\frac{2}{8}$$

Additive inverse =
$$-\frac{2}{8}$$

(ii)
$$-\frac{5}{9}$$

$${\rm Additive\ inverse\ =\ }\frac{5}{9}$$

$$\frac{-6}{-5} = \frac{6}{5}$$

Additive inverse =
$$\frac{-6}{5}$$

$$\frac{2}{(iv)} = \frac{-2}{9}$$

$$\begin{array}{l} = \frac{2}{9} \\ \text{Additive inverse} \end{array}$$

$$\frac{19}{(v)} = \frac{-19}{6}$$

$${\rm Additive\; inverse} = \frac{19}{6}$$

Question 3:

Verify that -(-x) = x for.

$$x = \frac{11}{15}$$
 (ii) $x = -\frac{13}{17}$

Answer:

(i)
$$x = \frac{11}{15}$$

The additive inverse of
$$x = \frac{11}{15}$$
 is $-x = -\frac{11}{15}$ as $\frac{11}{15} + \left(-\frac{11}{15}\right) = 0$

$$\frac{11}{15} + \left(-\frac{11}{15}\right) = 0$$
 This equality
$$\frac{11}{15} + \left(-\frac{11}{15}\right) = 0$$
 represents that the additive inverse of
$$-\frac{11}{15} = \frac{11}{15}$$
 or it

can be said that
$$-\left(-\frac{11}{15}\right) = \frac{11}{15}$$
 i.e., $-(-x) = x$

(ii)
$$x = -\frac{13}{17}$$

$$x = -\frac{13}{17} \text{ is } -x = \frac{13}{17} \text{ as } -\frac{13}{17} + \frac{13}{17} = 0$$
 The additive inverse of

This equality
$$-\frac{13}{17} + \frac{13}{17} = 0$$
 represents that the additive inverse of $\frac{13}{17}$ is $-\frac{13}{17}$ i.e., $-(-x) = x$

Question 4:

Find the multiplicative inverse of the following.

$$_{(i)}$$
 -13 $_{(ii)}$ $\frac{-13}{19}_{(iii)}$ $\frac{1}{5}$

$$\frac{-5}{8} \times \frac{-3}{7}_{(v)} -1 \times \frac{-2}{5}_{(vi)} -1$$

Answer:

$$(i) -13$$

$$\mbox{Multiplicative inverse} = -\frac{1}{13}$$

$$\begin{array}{l} \text{Multiplicative inverse} = -\frac{19}{13} \end{array}$$

Multiplicative inverse = 5

$$\frac{5}{(iv)} - \frac{5}{8} \times -\frac{3}{7} = \frac{15}{56}$$

$$\frac{56}{\text{Multiplicative inverse}} = \frac{56}{15}$$

$$-1 \times -\frac{2}{5} = \frac{2}{5}$$

$$\begin{array}{l} \text{Multiplicative inverse} = \frac{5}{2} \end{array}$$

$$(vi) -1$$

Multiplicative inverse = -1

Question 5:

Name the property under multiplication used in each of the following:

(i)
$$\frac{-4}{5} \times 1 = 1 \times \frac{-4}{5} = -\frac{4}{5}$$

(ii)
$$-\frac{13}{17} \times \frac{-2}{7} = \frac{-2}{7} \times \frac{-13}{17}$$

$$\frac{-19}{29} \times \frac{29}{-19} = 1$$

Answer:

(i)
$$-\frac{4}{5} \times 1 = 1 \times -\frac{4}{5} = -\frac{4}{5}$$

1 is the multiplicative identity.

- (ii) Commutativity
- (iii) Multiplicative inverse

Question 6:

$$\frac{6}{13} \, \mathrm{by} \; \mathrm{the} \; \mathrm{reciprocal} \; \mathrm{of} \, \frac{-7}{16} \, .$$
 Multiply

$$\frac{6}{13} \times \left(\text{Reciprocal of } -\frac{7}{16} \right) = \frac{6}{13} \times -\frac{16}{7} = -\frac{96}{91}$$

Question 7:

Tell what property allows you to compute
$$\frac{1}{3} \times \left(6 \times \frac{4}{3}\right)$$
 as $\left(\frac{1}{3} \times 6\right) \times \frac{4}{3}$.

Answer:

Associativity

Question 8:

Is
$$\frac{8}{9}$$
 the multiplicative inverse of $-1\frac{1}{8}$? Why or why not?

Answer:

If it is the multiplicative inverse, then the product should be 1.

However, here, the product is not 1 as

$$\frac{8}{9} \times \left(-1\frac{1}{8}\right) = \frac{8}{9} \times \left(-\frac{9}{8}\right) = -1 \neq 1$$

Question 9:

Is 0.3 the multiplicative inverse of $3\frac{1}{3}$? Why or why not?

Answer:

$$3\frac{1}{3} = \frac{10}{3}$$

$$3\frac{1}{3} = 0.3 \times \frac{10}{3} = \frac{3}{10} \times \frac{10}{3} = 1$$

Here, the product is 1. Hence, 0.3 is the multiplicative inverse of $\frac{3\frac{1}{3}}{3}$. Question 10:

Write:

- The rational number that does not have a reciprocal.
- (ii) The rational numbers that are equal to their reciprocals.
- (iii) The rational number that is equal to its negative.

Answer:

- (i) 0 is a rational number but its reciprocal is not defined.
- (ii) 1 and -1 are the rational numbers that are equal to their reciprocals.
- (iii) 0 is the rational number that is equal to its negative.

Question 11:

Fill in the blanks.

- (i) Zero has _____ reciprocal.
- (ii) The numbers _____ and ____ are their own reciprocals
- (iii) The reciprocal of 5 is ______.

- (iv) Reciprocal of $\frac{1}{x}$, where $x \neq 0$ is
- (v) The product of two rational numbers is always a
- (vi) The reciprocal of a positive rational number is ____

Answer:

- (i) No
- (ii) 1, -1

- (iv) x
- (v) Rational number
- (vi) Positive rational number